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#### Cancer

- Cancer is the second leading cause of death in the United States, with an estimated **570,000 deaths** in 2013
- Over **1.6 million new cases** of cancer will be diagnosed in the United States in 2013
- In the world, cancer is also a leading cause of death **8.2 million deaths** in 2012

# Radiation Therapy

- Cancer can be treated using radiation therapy (RT)
- In RT, beams of high energy photons are fired into the patient that are able to kill cancerous cells
- **patients** undergo some form of radiation therapy • In the United States, about **half of all cancer**

# History of Radiation Therapy

- X-rays were discovered by Wilhelm Röntgen in 1895 (awarded the first Nobel Prize in Physics in 1901)
	- Shortly after, x-rays started being used to treat skin cancers
- Radium discovered by Marie and Pierre Curie in 1898 (Nobel Prize in Chemistry in 1911)
	- Began to be used to treat cancer, as well as other diseases



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# History of Radiation Therapy

- First radiation delivery machines (linear accelerators) developed in 1940
- Computed tomography (CT) invented in 1971
- **Invention of intensitymodulated radiation therapy (IMRT) in early 1980s**

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### IMRT

- To reach the tumor, radiation passes through healthy tissue, and damages both healthy and cancerous tissue
- Damage to healthy tissue can lead to undesirable side effects that reduce post-treatment quality of life
- We want the dose to "fit" the tumor as closely as possible, to reduce the dose to healthy tissues

### IMRT

- In IMRT, the intensity profile of each beam is nonuniform
- By using non-uniform intensity profiles, the threedimensional shape of the dose can better fit the tumor
- Let's see what this looks like

# Using Traditional Radiation Therapy



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# Using IMRT



# Using IMRT



# Designing an IMRT Treatment

- Fundamental problem:
	- How should the beamlet intensities be selected to deliver a therapeutic dose to the tumor *and* to minimize damage to healthy tissue?

### The Data

- Treatment planning starts from a CT scan
	- A radiation oncologist contours (draws outlines) around the tumor and various critical structures
	- Each structure is discretized into voxels (volume elements) – typically 4 mm x 4 mm x 4 mm
- From CT scan, can compute how much dose each beamlet delivers to every voxel



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### Small Example – 9 Voxels, 6 Beamlets



- Minimize total dose to healthy tissue (spinal  $+$  other)
- Constraints: tumor voxels at least 7Gy (Gray), spinal cord voxel at most 5Gy

#### Dose to Each Voxel – Beamlets 1, 2, 3



#### Dose to Each Voxel – Beamlets 4, 5, 6



# Small Example – The Model





Decisions:  $X_1, X_2, X_3, X_4, X_5, X_6$ 

Minimize  $(1+2)x_1 + (2+2.5)x_2 + 2.5x_3 + x_4 + 2x_5 + (1+2+1)x_6$  $2x_1 + x_5 \geq 7$  $x_{2} + 2x_{4} \ge 7$  $1.5x_3 + x_4 \ge 7$  $1.5x_3 + x_5 \geq 7$  $2x_{2} + 2x_{5} \le 5$  $x_1, x_2, x_3, x_4, x_5, x_6 > 0$ 

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# A Head and Neck Example

- We will test out this approach on a head-and-neck case
	- Total of 132,878 voxels
	- One target volume  $(9,777)$ voxels)
	- Five critical structures: spinal cord, brain, brain stem, parotid glands, mandible (jaw)
	- 5 beams; each beam  $~1$ 60 beamlets (1cm x 1cm) for a total of 328 beamlets





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## Treatment Plan Criteria

- Dose to whole tumor between 70Gy and 77Gy
- Maximum spinal cord dose at most 45Gy
	- Significant damage to any voxel will result in loss of function
- Maximum brain stem dose at most 54Gy
- Maximum mandible dose at most 70Gy
- Mean parotid gland dose at most 26Gy
	- Parotid gland is a parallel structure: significant damage to any voxel does not jeopardize function of entire organ

## The Optimization Problem

#### minimize Total healthy tissue dose

subject to  $70 \text{Gy} \leq \text{Dose}$  to voxel  $v \leq 77 \text{Gy}$ , for all tumor voxels v, Dose to voxel  $v \leq 45 \text{Gy}$ , for all spinal cord voxels v, Dose to voxel  $v \leq 54\text{Gy}$ , for all brain stem voxels v, Dose to voxel  $v \leq 70 \text{Gy}$ , for all mandible voxels v, Total parotid dose<br>Num. parotid voxels  $\leq$  26Gy,  $w_b \geq 0$ , for all beamlets b.

#### Solution



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# Exploring Different Solutions

- Mean mandible dose was  $11.3G_y$  how can we reduce this?
- One approach: modify objective function
	- Current objective is the sum of the total dose  $T_{\rm B}+T_{\rm BS}+T_{\rm SC}+T_{\rm PG}+T_{\rm M}$
	- Change objective to

 $T_{\rm B}+T_{\rm BS}+T_{\rm SC}+T_{\rm PC}+10\times T_{\rm M}$ 

• Set mandible weight from 1 (current solution) to 10

#### New Solution



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### Sensitivity

- Another way to explore tradeoffs is to modify constraints
	- For example: by relaxing the mandible maximum dose constraint, we may improve our total healthy tissue dose
	- How much does the objective change for different constraints?

# Shadow Prices



- Parotid gland and brain stem have shadow prices of zero
	- Modifying these constraints is not beneficial
- Mandible has highest shadow price
	- If slight increase in mandible dose is acceptable, total healthy tissue dose can be significantly reduced

## IMRT Optimization in Practice

- Radiation machines are connected to treatment planning software that implements and solves optimization models (linear and other types)
	- Pinnacle by Philips
	- RayStation by RaySearch Labs
	- Eclipse by Varian

#### Extensions

#### • Selection of beam angles

- Beam angles can be selected jointly with intensity profiles using **integer optimization** (topic of next week)
- Uncertainty
	- Often quality of IMRT treatments is degraded due to uncertain organ motion (e.g., in lung cancer, patient breathing)
		- Can manage uncertainty using a method known as **robust optimization**

## **Efficiency**

- Manually designing an IMRT treatment is inefficient and impractical
- Linear optimization provides an *efficient* and *systematic*  way of designing an IMRT treatment
	- Clinical criteria can often be modeled using constraints
	- By changing the model, treatment planner can explore tradeoffs

### Clinical Benefits

- Ultimately, IMRT benefits the patient
- In head and neck cancers, saliva glands were rarely spared prior to IMRT; optimized IMRT treatments spare saliva glands
- In prostate cancer, optimized IMRT treatments reduce toxicities and allow for higher tumor doses to be delivered safely
- In lung cancer, optimized IMRT reduces risk of radiation-induced pneumonitis

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