RADIATION THERAPY An Application of Linear Optimization

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Cancer

- Cancer is the second leading cause of death in the United States, with an estimated 570,000 deaths in 2013
- Over **1.6 million new cases** of cancer will be diagnosed in the United States in 2013
- In the world, cancer is also a leading cause of death –
 8.2 million deaths in 2012

Radiation Therapy

- Cancer can be treated using radiation therapy (RT)
- In RT, beams of high energy photons are fired into the patient that are able to kill cancerous cells
- In the United States, about **half of all cancer patients** undergo some form of radiation therapy

History of Radiation Therapy

- X-rays were discovered by Wilhelm Röntgen in 1895 (awarded the first Nobel Prize in Physics in 1901)
 - Shortly after, x-rays started being used to treat skin cancers
- Radium discovered by Marie and Pierre Curie in 1898 (Nobel Prize in Chemistry in 1911)
 - Began to be used to treat cancer, as well as other diseases



History of Radiation Therapy

- First radiation delivery machines (linear accelerators) developed in 1940
- Computed tomography (CT) invented in 1971
- Invention of intensitymodulated radiation therapy (IMRT) in early 1980s

Machines and MRI scan images removed due to copyright restrictions.

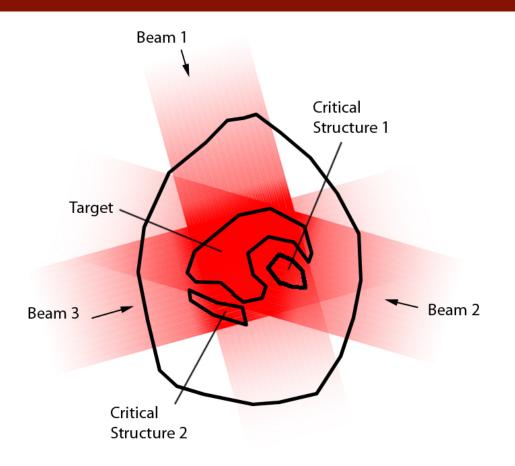
IMRT

- To reach the tumor, radiation passes through healthy tissue, and damages both healthy and cancerous tissue
- Damage to healthy tissue can lead to undesirable side effects that reduce post-treatment quality of life
- We want the dose to "fit" the tumor as closely as possible, to reduce the dose to healthy tissues

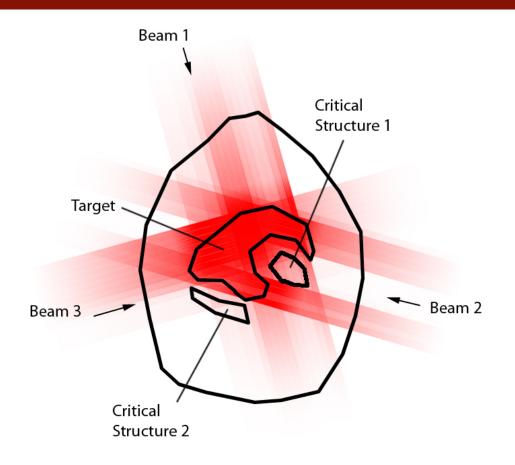
IMRT

- In IMRT, the intensity profile of each beam is nonuniform
- By using non-uniform intensity profiles, the threedimensional shape of the dose can better fit the tumor
- Let's see what this looks like

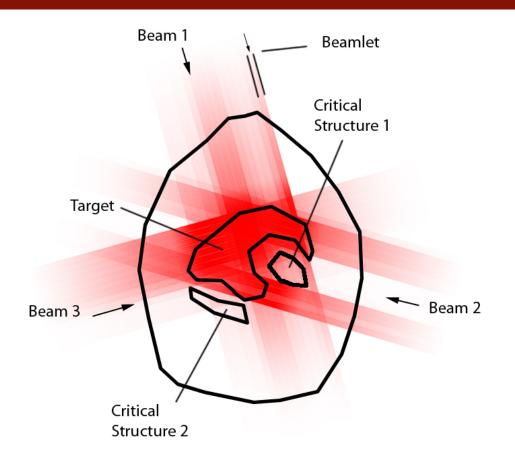
Using Traditional Radiation Therapy



Using IMRT



Using IMRT

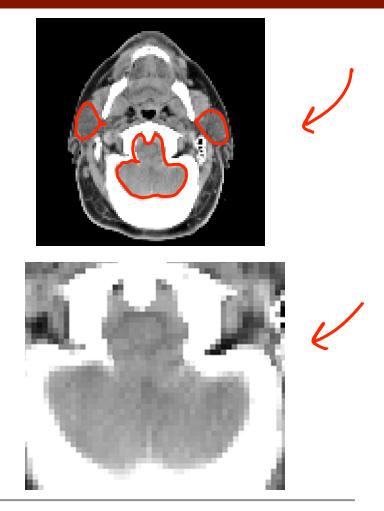


Designing an IMRT Treatment

- Fundamental problem:
 - How should the beamlet intensities be selected to deliver a therapeutic dose to the tumor *and* to minimize damage to healthy tissue?

The Data

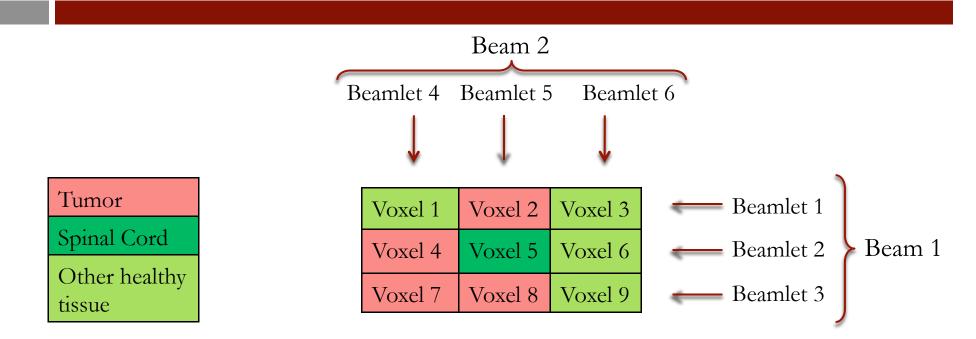
- Treatment planning starts from a CT scan
 - A radiation oncologist contours (draws outlines) around the tumor and various critical structures
 - Each structure is discretized into voxels (volume elements) – typically 4 mm x 4 mm x 4 mm
- From CT scan, can compute how much dose each beamlet delivers to every voxel



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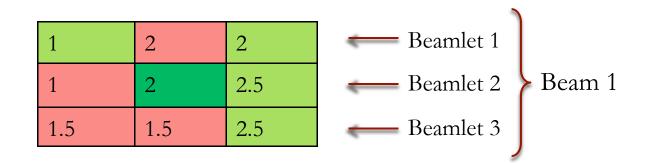
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Small Example – 9 Voxels, 6 Beamlets

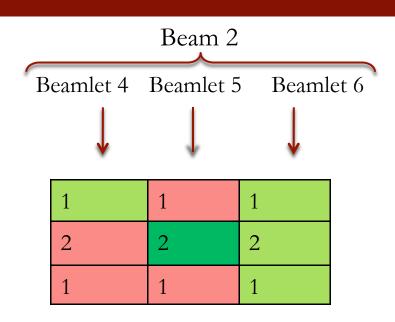


- Minimize total dose to healthy tissue (spinal + other)
- Constraints: tumor voxels at least 7Gy (Gray), spinal cord voxel at most 5Gy

Dose to Each Voxel – Beamlets 1, 2, 3

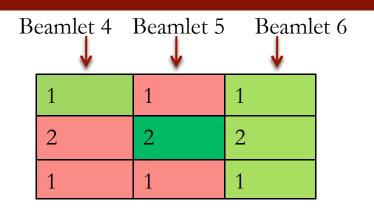


Dose to Each Voxel – Beamlets 4, 5, 6



Small Example – The Model

1	2	2	-	Beamlet 1
1	2	2.5	~	Beamlet 2
1.5	1.5	2.5	←	Beamlet 3



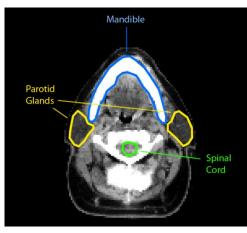
Decisions: X1, X2, X3, X4, X5, X6

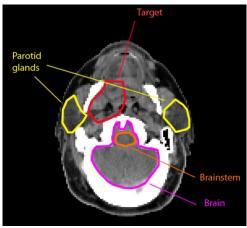
Minimize $(1+2)X_1 + (2+2.5)X_2 + 2.5X_3 + X_4 + 2X_5 + (1+2+1)X_6$ $2X_1 + X_5 \ge 7$ $X_2 + 2X_4 \ge 7$ $(.5X_3 + X_4 \ge 7)$ $1.5X_3 + X_5 \ge 7$ $2X_2 + 2X_5 \le 5$ $X_1, X_2, X_3, X_4, X_5, X_6 \ge 0$

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A Head and Neck Example

- We will test out this approach on a head-and-neck case
 - Total of 132,878 voxels
 - One target volume (9,777 voxels)
 - Five critical structures: spinal cord, brain, brain stem, parotid glands, mandible (jaw)
 - 5 beams; each beam ~60 beamlets (1cm x 1cm) for a total of 328 beamlets





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Treatment Plan Criteria

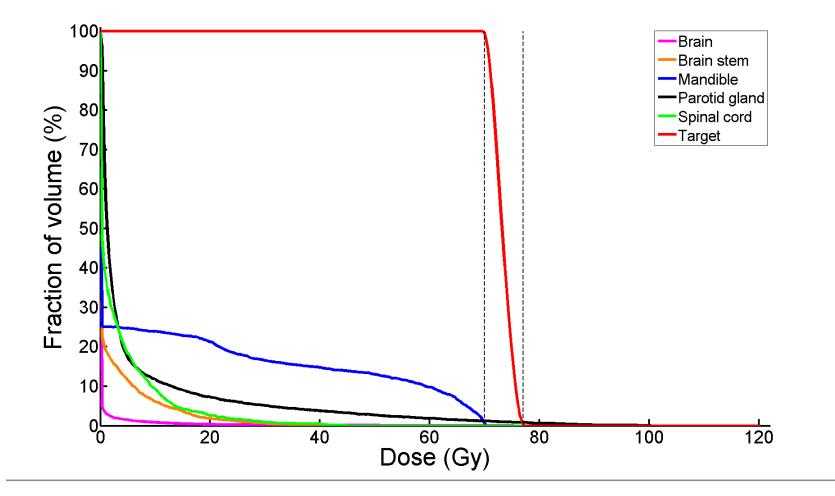
- Dose to whole tumor between 70Gy and 77Gy
- Maximum spinal cord dose at most 45Gy
 - Significant damage to any voxel will result in loss of function
- Maximum brain stem dose at most 54Gy
- Maximum mandible dose at most 70Gy
- Mean parotid gland dose at most 26Gy
 - Parotid gland is a parallel structure: significant damage to any voxel does not jeopardize function of entire organ

The Optimization Problem

minimize Total healthy tissue dose

subject to $70\text{Gy} \leq \text{Dose}$ to voxel $v \leq 77\text{Gy}$, for all tumor voxels v, Dose to voxel $v \leq 45\text{Gy}$, for all spinal cord voxels v, Dose to voxel $v \leq 54\text{Gy}$, for all brain stem voxels v, Dose to voxel $v \leq 70\text{Gy}$, for all mandible voxels v, $\frac{\text{Total parotid dose}}{\text{Num. parotid voxels}} \leq 26\text{Gy},$ $w_b \geq 0$, for all beamlets b.

Solution



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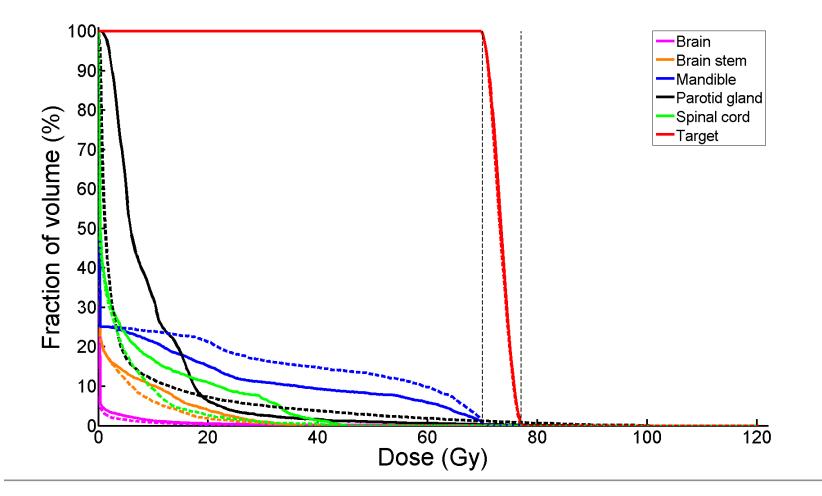
Exploring Different Solutions

- Mean mandible dose was 11.3Gy how can we reduce this?
- One approach: modify objective function
 - Current objective is the sum of the total dose $T_{\rm B}+T_{\rm BS}+T_{\rm SC}+T_{\rm PG}+T_{\rm M}$
 - Change objective to

 $T_{\rm B} + T_{\rm BS} + T_{\rm SC} + T_{\rm PG} + 10 \times T_{\rm M}$

• Set mandible weight from 1 (current solution) to 10

New Solution



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Sensitivity

- Another way to explore tradeoffs is to modify constraints
 - For example: by relaxing the mandible maximum dose constraint, we may improve our total healthy tissue dose
 - How much does the objective change for different constraints?

Shadow Prices

Organ	Highest shadow price
Parotid gland	0
Spinal cord	96.911
Brain stem	0
Mandible	7399.72

- Parotid gland and brain stem have shadow prices of zero
 - Modifying these constraints is not beneficial
- Mandible has highest shadow price
 - If slight increase in mandible dose is acceptable, total healthy tissue dose can be significantly reduced

IMRT Optimization in Practice

- Radiation machines are connected to treatment planning software that implements and solves optimization models (linear and other types)
 - Pinnacle by Philips
 - RayStation by RaySearch Labs Eclipse by Varian

Extensions

- \rightarrow Selection of beam angles
 - Beam angles can be selected jointly with intensity profiles using **integer optimization** (topic of next week)
 - Uncertainty
 - Often quality of IMRT treatments is degraded due to uncertain organ motion (e.g., in lung cancer, patient breathing)
 - Can manage uncertainty using a method known as **robust optimization**

Efficiency

- Manually designing an IMRT treatment is inefficient and impractical
- Linear optimization provides an *efficient* and *systematic* way of designing an IMRT treatment
 - Clinical criteria can often be modeled using constraints
 - By changing the model, treatment planner can explore tradeoffs

Clinical Benefits

- Ultimately, IMRT benefits the patient
- In head and neck cancers, saliva glands were rarely spared prior to IMRT; optimized IMRT treatments spare saliva glands
- In prostate cancer, optimized IMRT treatments reduce toxicities and allow for higher tumor doses to be delivered safely
- In lung cancer, optimized IMRT reduces risk of radiation-induced pneumonitis

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