

# Types for Information Flow

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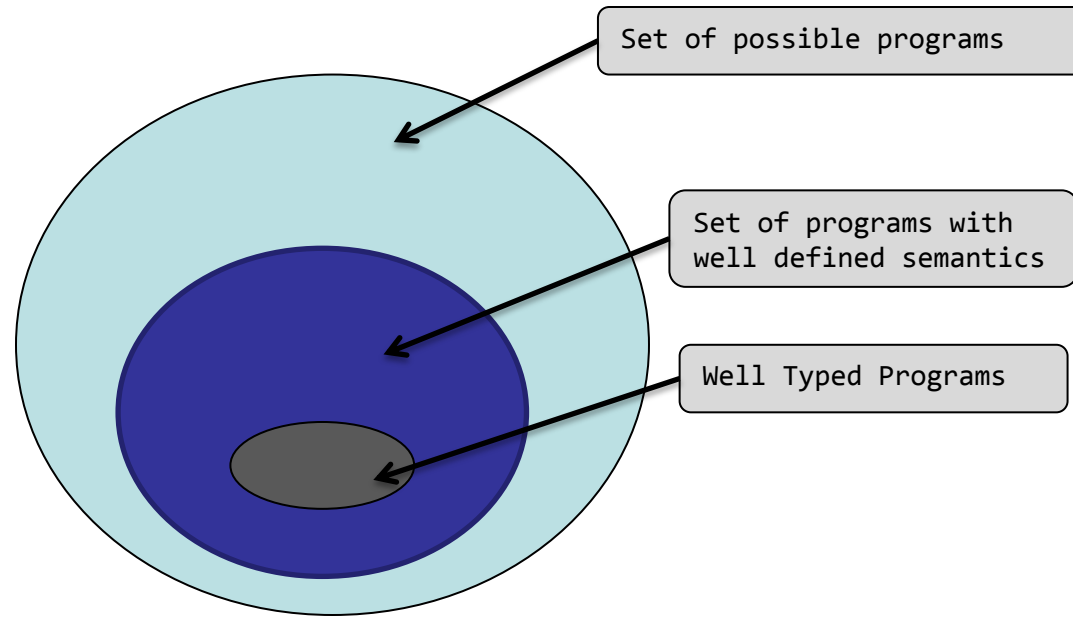
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Based on the paper by Myers, A. C. “JFlow: practical mostly-static information flow control”. In POPL '99

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# Recap

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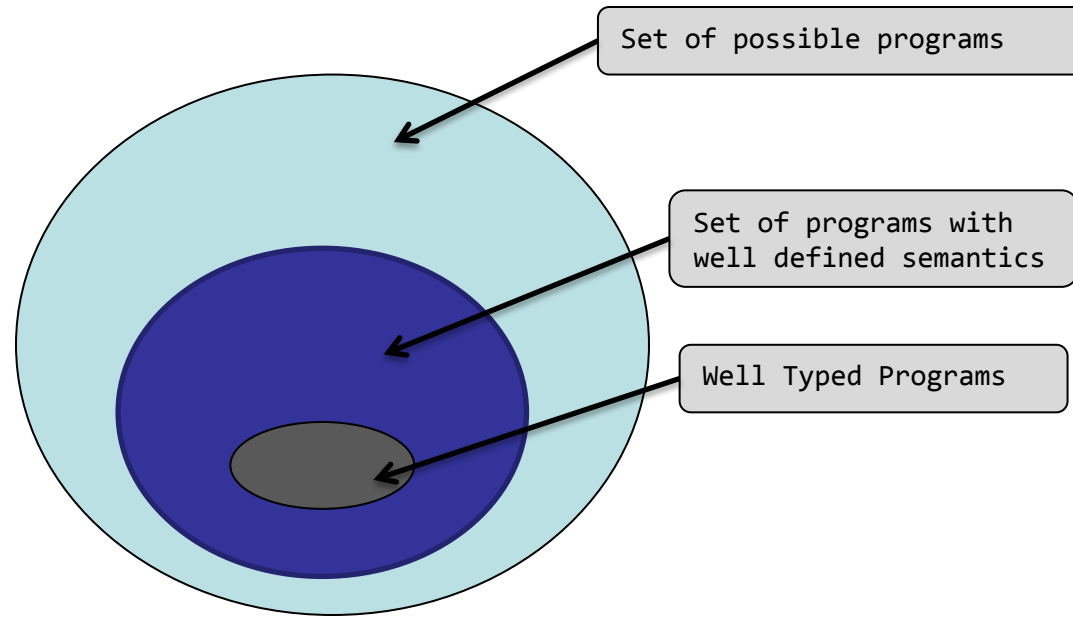


## Functional World:

- evaluation proceeds through reduction rules
- types impose constraints on the shape of the program
- a program with a legal shape (according to the type system)
  - always has an available reduction rule (unless it has terminated)
  - the reduction rule will produce a new program with a legal shape

# Recap

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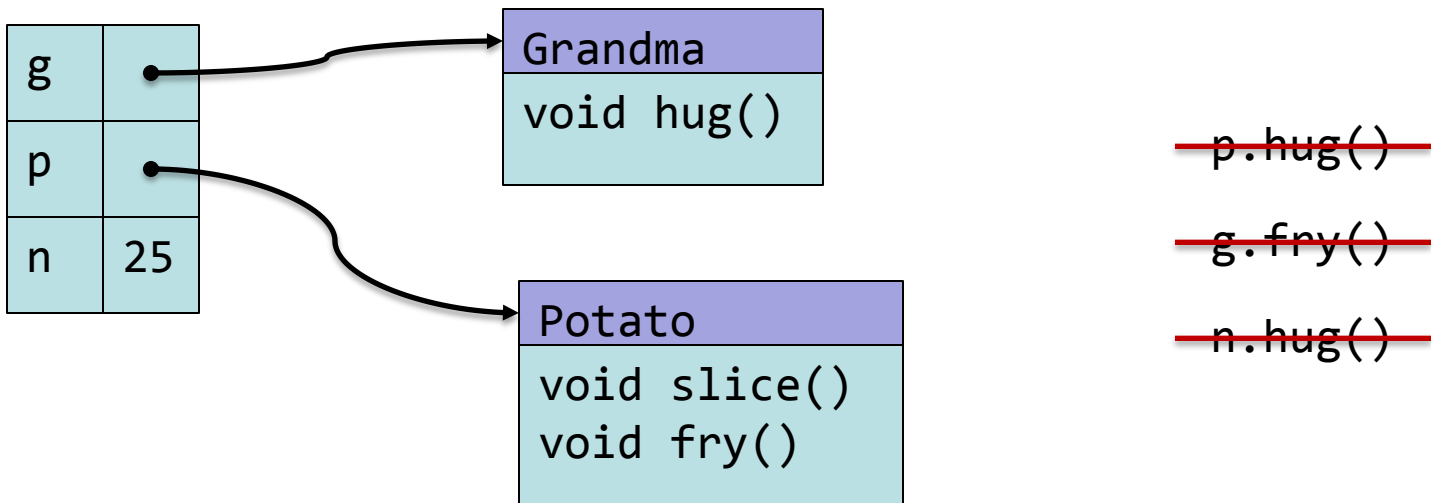


## Imperative World:

- evaluation involves updating a store
- types place restrictions on the program store
  - this allows static reasoning about legal operations on the objects in the store

# Recap

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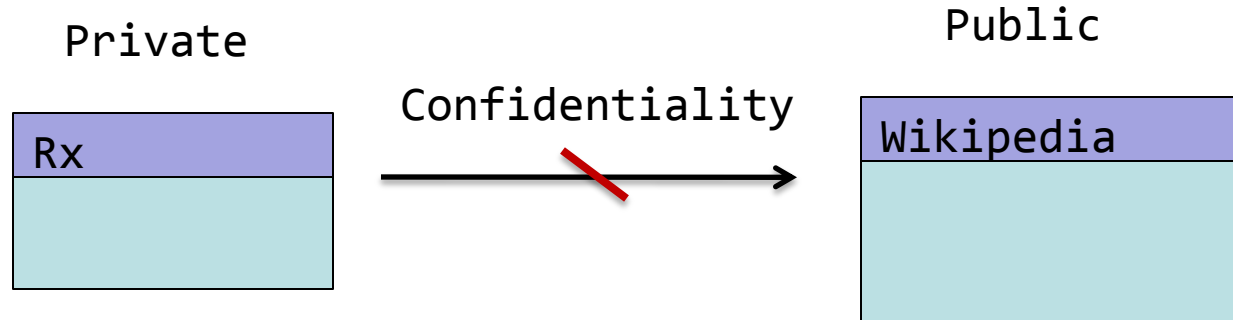


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  - this allows static reasoning about legal operations on the objects in the store

# Enforcing Security Properties

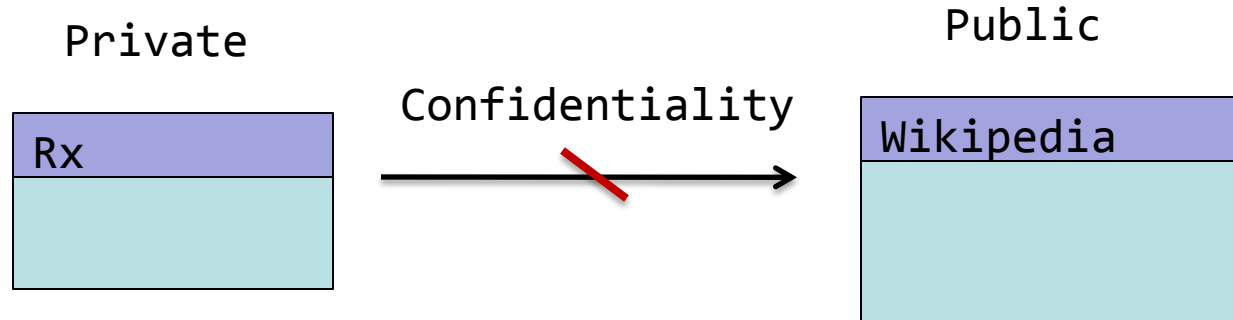
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```
Rx myrx = getMyRx();  
Wikipedia w = getWPEntry("Armando");  
  
w.addEntry(myrx.toString());
```

```
w.write("YES");
```

# Enforcing Security Properties



```
Rx myrx = getMyRx();
Wikipedia w = getWPEntry("Armando");

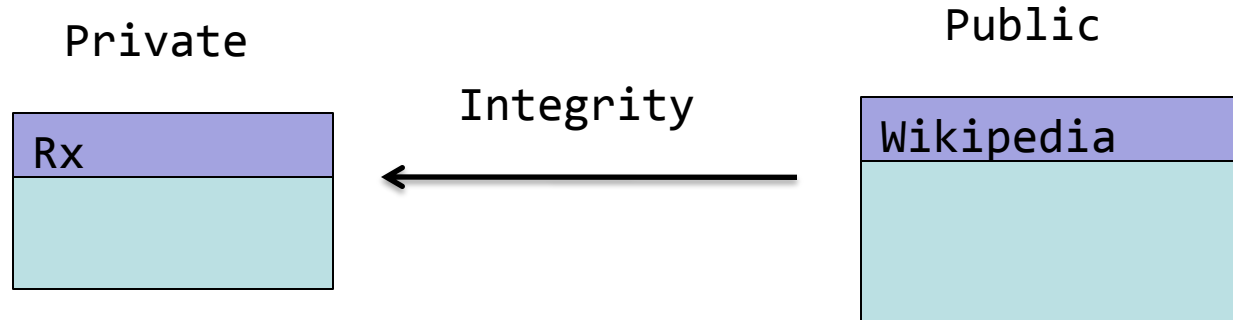
w.write("Hemorrhoids :");
p.val = myrx.contains("Preparation H");
if(q.val){
    w.write("YES");
}
```

If  $p=q$  information clearly leaks

Even if  $p \neq q$ , information can still leak if  $p \neq q$  was caused by some information about `myrx`.

# Enforcing Security Properties

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```
class Doctor{  
    Rx cureFlu(){  
        Rx myrx = new Rx();  
        Wikipedia w = getWPEntry("Flu");  
        myrx.set(w.getSubEntry("Treatment"));  
        return myrx;  
    }  
}
```

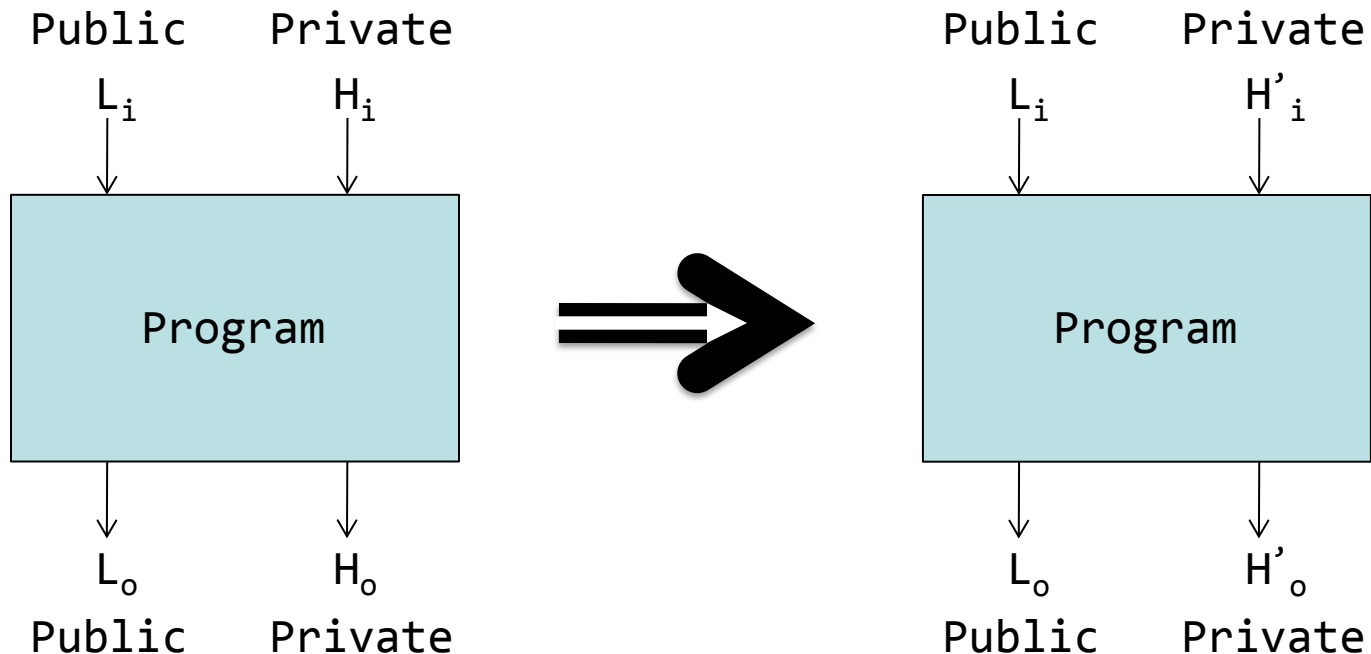
# What is information flow?

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If there is no information flow from private to public, then a change in a private input can not affect a public output

- you can't determine this from a single execution

For all  $L_i, H_i, H'_i$





# Solution Strategy

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We proceed through the following two steps

- Define a dynamic labeling scheme so that at any given time, the labels in a piece of data tell us whether it's OK to leak it or not.
  - Labels turn a global property about all executions into a local property in a conservative way
  - This will be the dynamic semantics against which we can prove type safety.
- Define a type system that allows us to approximate the set of labels that the data pointed at by a variable can have.
  - If an action is ok according to the conservative approximation, we know it would be ok according to the dynamic scheme.

# Labeling Data With Security Policies

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Policies for information flow

Owner: reader1, reader2, reader3

- “according to owner, this data can only be read by reader1, reader2, or reader3”

Label { policy1, policy2, policy3 }

- If an owner is not mentioned, it is assumed she has no privacy concerns

Why do we need an owner?

Revocation

# Principals

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Owners and readers are principals

- user, group or role

act\_for relationship

- allows principals to act for other principals

Armando act\_for Faculty

# Labels form a lattice

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$$L1 \leq L2$$

L1 can be relabeled to L2

- means that L2 is more restrictive (fewer readers)
- Warning: this is counterintuitive
  - L2 actually has fewer readers.

Partial Order defines a lattice

- Least upper bound  $\sqcup$
- Least fixed point
- bottom

If a variable is certified to handle data with L2 labels correctly, we can trust that variable to hold a value with label L1

- Just like subtyping!

# Labels form a lattice

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## Question

$$\{\text{Joe: Ann, Jill}\} \leq \{\text{Joe:Ann}\}$$

$$\{\text{Joe: (Ann, Jill), Tim:Ann}\} \leq \{\text{Joe:(Ann), Tim:Ann}\}$$

$$\{\text{Joe: (Ann), Tim:Ann}\} \quad ??? \quad \{\text{Joe:(Ann)}\}$$

# Assignment

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$x\{L2\} := v\{L1\};$

$L1 \leq L2$

Can only assign to a variable to a more restrictive label

# Binary Operations

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`a{L1} + b{L2};`

Trick question:

- What should be the label for `a+b`?

```
int{Joe:everyone} a, b, c;  
...  
int{Joe:Joe} p;  
c = 0;  
if(p){  
    c = a + b;  
}
```

- What information would be leaked if this code were to execute?

# Information flow through control

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## Information flow through the PC

- We need to keep track of the information that is leaked just from knowing that the computation reached a particular point.

```
int{Joe:everyone} a, b, c;  
...  
int{Joe:Joe} p;  
→ c = 0;  
→ if(p){  
    c = a + b;  
→ }
```

PC Label

{}
{Joe:Joe}

Simple scheme except for non-structured control

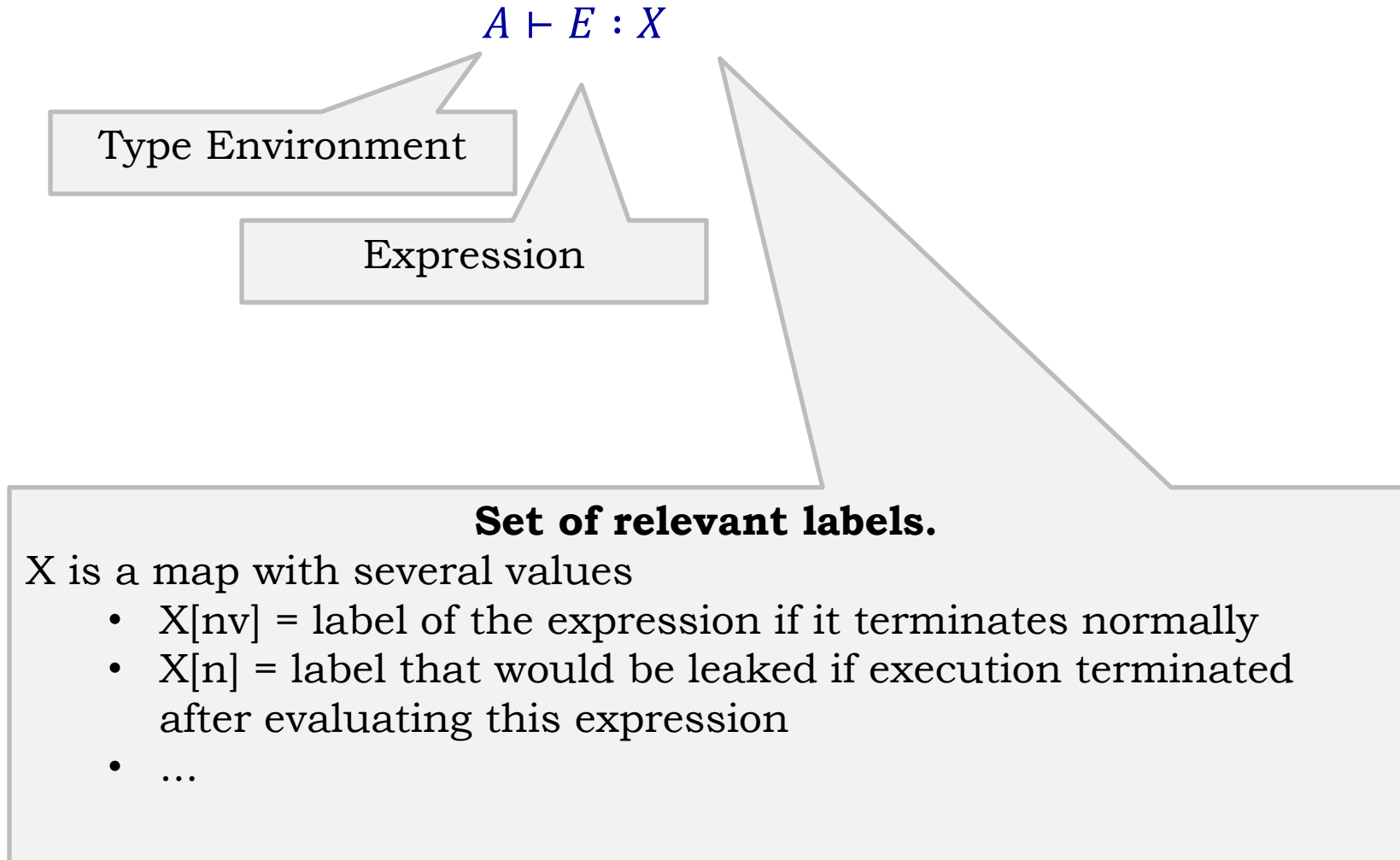
- return, continue, throw, break



# Formalizing the type system

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## Basic judgments



# Rules

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*true*

---

$$A \vdash literal : X_{\emptyset}[\underline{n} := A[\underline{pc}], \underline{nv} := A[\underline{pc}]]$$

If evaluating a literal somehow caused the program to terminate, I would leak the pc label.

The value of the literal also carries information about the PC label.

```
if(p){  
  x = literal  
}
```

This is what prevents the code above from leaking information; the assignment only type checks if x is compatible with the PC label

# Rules

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$$\frac{A[v] = \langle \text{var} \ [\text{final}] \ T\{L\} \ \text{uid} \rangle \quad X = X_{\emptyset} [\underline{n} := A[\underline{\text{pc}}], \underline{\text{nv}} := L \sqcup A[\underline{\text{pc}}]]}{A \vdash v : X}$$

Least upper bound. The return value must carry the labels of both the variable and the pc.

# Rules

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$$\frac{A \vdash E : X \quad A[v] = \langle \text{var } T\{L\} \text{ uid} \rangle \quad A \vdash X[\underline{nv}] \sqsubseteq L}{A \vdash v = E : X}$$

This is the label of expression E.  
It has to be less restrictive than L

# Rules

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$$\frac{\begin{array}{l} A \vdash E : X_E \\ A[\underline{\text{pc}} := X_E[\underline{\text{nv}}]] \vdash S_1 : X_1 \\ A[\underline{\text{pc}} := X_E[\underline{\text{nv}}]] \vdash S_2 : X_2 \\ X = X_E[\underline{\text{n}} := \underline{\emptyset}] \oplus X_1 \oplus X_2 \end{array}}{A \vdash \text{if } (E) S_1 \text{ else } S_2 : X}$$

This computes the join of  $X_E$ ,  $X_1$ ,  $X_2$ , except we don't care about  $X_E[\text{n}]$  so we set it to  $\{\}$ .

# Rules

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extend the environment to add  
any new variable declarations

update PC in the new  
environment

$$\frac{\begin{array}{c} A \vdash S_1 : X_1 \\ \text{extend}(A, S_1)[\underline{\text{pc}} := X_1[\underline{n}]] \vdash S_2 : X_2 \\ X = X_1[\underline{n} := \underline{\emptyset}] \oplus X_2 \end{array}}{A \vdash S_1; S_2 : X}$$

# Example

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$x \{ \text{Joe: Erika} \} = \{ \text{Joe: Erika, Peter} \}$

$\text{if}(x)\{$

$\quad p\{ \text{Tim:Erika, Joe:Erika} \} = \{ \text{Tim: Everyone} \}$

$\}$

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