

In order to satisfy the static discipline, a circuit must produce outputs that are better than the acceptable inputs.

This ensures that if you concatenate multiple gates together, for example one buffer followed by another buffer, then the input to each gate will be valid even if a small amount of noise was introduced by the previous gate.

So taking a closer look at that, what that means is that if I have a valid input at my first buffer, and I am guaranteeing that the output that I produce is slightly better than my original input, then even if a little bit of noise was introduced, the input to the second buffer is still going to be considered a valid input.

More concretely, to satisfy the static discipline, a valid low output must be less than a valid low input.

The way that we specify this is that is that $V_{ol} < V_{il}$.

Also, a valid high output must be greater than a valid high input.

So $V_{oh} > V_{ih}$.

If we put this all together, we have $V_{ol} < V_{il}$ and $V_{oh} > V_{ih}$ and of course we want our low inputs to be less than or equal to our high inputs, so $V_{il} < V_{ih}$.

Another way to think about this is to look at the orange and green arrows which show the ranges of valid inputs which are wider than the ranges of valid outputs.

The other thing that is shown here are the noise margins which correspond to the area of valid inputs but invalid outputs.

As we said earlier, a valid input must always produce a valid output.

A valid input has $V_{in} < V_{il}$ if its low or $V_{in} > V_{ih}$ if its high.

A valid output has $V_{out} < V_{ol}$ if its low and $V_{out} > V_{oh}$ if its high.

In this problem, we want to determine whether specifications 1, 2, and 3 (which provide 0.3 volt noise margins) satisfy the static discipline given the voltage transfer curve shown here.

For each specification, we need to check the following two constraints: 1) Is $V_{ol} < V_{il} < V_{ih} < V_{oh}$ - satisfying this constraint guarantees that the outputs produced are better in quality than the inputs.

The second constraint is: Does a valid input produce a valid output?

Since this curve shows an inverting function, this translates to: a) Does a valid input (where $V_{in} < V_{il}$) always produce

a valid high output (where $V_{out} > V_{oh}$)?

And b) Does a valid high input (where $V_{in} > V_{ih}$) always produce a valid low output (where $V_{out} \leq V_{ol}$)?

If all of these constraints are satisfied, then that specification obeys the static discipline.

If not, it doesn't.

For all three specifications, we see that indeed $V_{ol} \leq V_{ih} \leq V_{oh}$, so the first constraint is satisfied for all three specifications.

Now let's check the second constraint.

For specification #1: If $V_{in} \leq V_{ih}$ which is equal to 0.4, then $V_{out} = 5$ which is greater than V_{oh} which is 4.9, so a valid low input produces a valid high output.

If $V_{in} > V_{ih}$ which equals 4.6 then V_{out} equals 0 which is less than V_{ol} which is 0.1, so a valid high input produces a valid low output.

Since all of the constraints are satisfied, specification #1 satisfies the static discipline.

For specification #2: If $V_{in} \leq V_{ih}$ which is not greater than V_{oh} which is 4.4.

So this specification does not satisfy the static discipline.

For specification #3: If $V_{in} \leq V_{ih}$ which in this case is greater than V_{oh} which is 3.9.

So the first part of the constraint checks out.

Now we need to check what happens when we have a valid high input.

In this case, if $V_{in} > V_{ih}$ then $V_{out} \leq V_{ol}$ or 1.1, so this part of the constraint checks out as well.

Since all the constraints are satisfied, that means that specification #3 also satisfies the static discipline.