

a) Assuming L' is uniform across the span,

$$D_i' = L' \alpha_i = L' \frac{W}{V_\infty}$$

Given: $W = \frac{L}{2\rho V_\infty b^2}$

$$D_i = D_i' b = L' b \frac{W}{V} = L \frac{W}{V} = \frac{L^2}{2\rho V_\infty^2 b^2} = \frac{L^2}{\frac{1}{2}\rho V^2} \frac{1}{4b^2}$$

$$C_{D_i} = \frac{D_i}{\frac{1}{2}\rho V_\infty^2 S} = \frac{L^2}{(\frac{1}{2}\rho V_\infty^2)^2 S^2} \cdot \frac{S}{4b^2} = \frac{C_L^2}{4R}$$

b) $C_L = 2\pi \alpha_{\text{eff}} = 2\pi (\alpha - \alpha_i)$

ignore $\alpha_{L=0}$, no effect on $\frac{dC_L}{d\alpha}$

but we have $C_{D_i} = \alpha_i C_L$, or $\alpha_i = \frac{C_{D_i}}{C_L} = \frac{C_L}{4R}$

$$\Rightarrow C_L = 2\pi \left(\alpha - \frac{C_L}{4R} \right)$$

$$C_L \left(1 + \frac{\pi}{2R} \right) = 2\pi \alpha$$

$$C_L(\alpha) = \frac{2\pi}{1 + \frac{\pi}{2R}} \alpha$$

$$\frac{dC_L}{d\alpha} = \frac{2\pi}{1 + \frac{\pi}{2R}}$$

small than 2-D value of 2π
by factor of $\frac{1}{1 + \frac{\pi}{2R}}$

